



# APECE-302: Radio & Television Engineering

## Applied Physics, Electronics & Communication Engineering

Lecture # 04



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# Contents

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- Noise and its Classification
- Thermal Noise
- Shot Noise
- Addition of Noise from Different Sources
- Addition of Noise in Cascaded System
- Signal to Noise Ratio
- Noise Figure

# Noise and its classification

- Noise: Unwanted Signal
  
- External
  - Atmospheric/static
  - Extraterrestrial
  - Man-made
  
- Internal
  - Thermal
  - Shot
  - Transit time
  - Misc (Flicker, Transistor thermal, partition)

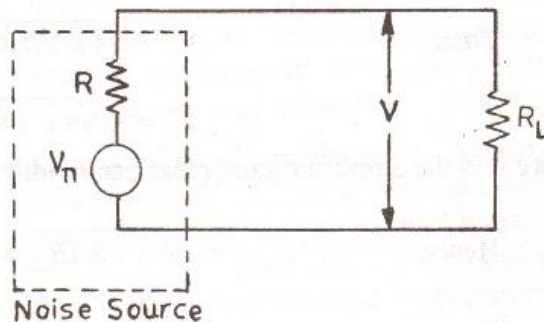
# Thermal noise

Noise Power:

$$P_n = \bar{k} T B$$

$\bar{k}$  is the Boltzmann constant ( $1.38 \times 10^{-23}$  Joule/deg. K)  
 $T$  is the absolute temperature, K = 273° + deg. C  
 $B$  is the bandwidth in hertz.

Resistor as a noise generator



$$P_n = \frac{V^2}{R_L} = \frac{V^2}{R} = \frac{(V_n / 2)^2}{R} = \frac{V_n^2}{4R}$$

$$V_n^2 = 4R P_n = 4R \bar{k} T B$$

$$V_n = \sqrt{4R \bar{k} T B}$$

# Thermal noise

A resistor of value  $20\text{ k}\Omega$  is connected at the input of an amplifier operating over the frequency range 10 to 11 MHz. Compute the rms noise voltage at the input of the amplifier if the ambient temperature is  $24^\circ\text{C}$ .



$$V_n = \sqrt{4kTRB} = \sqrt{4 \times 1.38 \times 10^{-23} \times (273 + 24) \times 20 \times 10^3 \times (11 - 10) \times 10^6} \text{ volt} = 18.1 \mu\text{V}.$$

The noise output of a resistor is amplified by a noiseless amplifier having gain of 40 and bandwidth of 40 KHz. A meter connected to the output of the amplifier reads 4 mV rms (a). If the resistor is operated at  $27^\circ\text{C}$ , what is its resistance? (b) If the bandwidth of the amplifier is reduced to 10 KHz, its gain remaining constant, what will the meter read now?



# Thermal noise

**Solution.** (a)  $V_n = \sqrt{4 \bar{k} TRB}$

Hence  $R = \frac{V_n^2}{4 \bar{k} TB}$

The rms noise voltage generated in the resistor  $= \frac{4 \text{ mV}}{40} = 100 \mu \text{ V}$

Hence  $R = \frac{(100 \times 10^{-6})^2}{4 \times 1.38 \times 10^{-23} \times (273 + 27) 40 \times 10^3} \Omega$

$$= 15.1 \times 10^6 \Omega$$

(b) Initially  $B = 40 \text{ kHz}$

Then  $V_n = \sqrt{4 \bar{k} TRB}$

$$V_o = A \sqrt{4 \bar{k} TRB}$$

where  $A$  is the amplifier gain. Next bandwidth is reduced to 10 kHz, i.e.  $B' = B/4$ .

Hence  $V_o = A \sqrt{4 \bar{k} TR (B/4)} = \frac{1}{2} A \sqrt{4 \bar{k} TRB} = \frac{1}{2} \times 4 \text{ mV} = 2 \text{ mV}.$

# Shot noise

For a diode, rms shot noise current:

$$I_n = \sqrt{2 q I_p B}$$

where  $q$  is the magnitude of the charge of an electron ( $1.6 \times 10^{-19}$  Coulomb)  
 $I_p$  is the direct diode current, Amp.  
and  $B$  is the bandwidth of the system, hertz.

Adding thermal noise and shot noise component??

Overcome by taking  $R_{eq}$

# Addition of noise due to several sources

Several thermal noise sources in series:

$$V_{n_1} = \sqrt{4 \bar{k} T B R_1}$$

$$V_{n_2} = \sqrt{4 \bar{k} T B R_2}$$

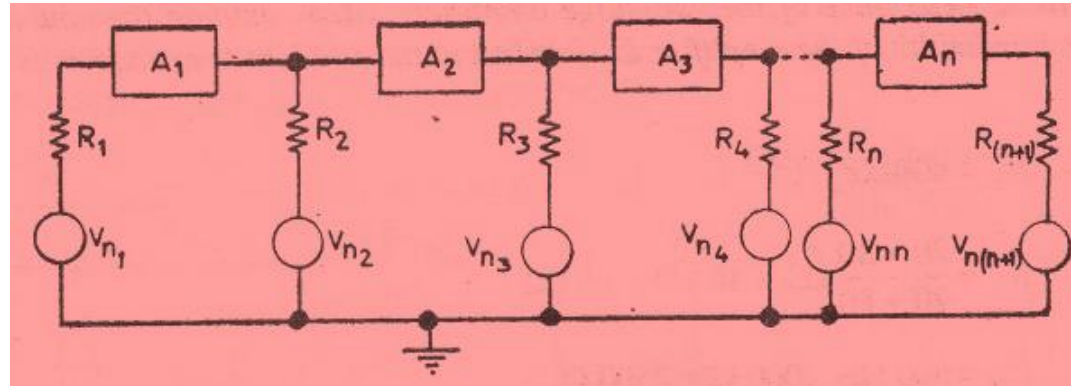
$$\begin{aligned} V_{nr} &= \sqrt{V_{n_1}^2 + V_{n_2}^2 + V_{n_3}^2 + \dots} = \sqrt{4 \bar{k} T B (R_1 + R_2 + R_3 + \dots)} \\ &= \sqrt{4 \bar{k} T B R} \end{aligned}$$

$$R = R_1 + R_2 + R_3 + \dots$$



# Addition of noise in cascaded amplifiers

Equivalent I/P noise voltage:



$$V_{n3} = \sqrt{4kTBR_3}$$

$$V_{n3}' = \frac{V_{n3}}{A_2} = \frac{\sqrt{4kTBR_3}}{A_2} = \sqrt{4kTBR_3'}$$

$$R_3' = \frac{R_3}{A_2^2}$$

$$R_{2'} = R_2 + R_3' = R_2 + \frac{R_3}{A_2^2}$$

$$R_2' = \frac{R_{2'}}{A_1^2} = \frac{R_2 + R_3/A_2^2}{A_1^2} = \frac{R_2}{A_1^2} + \frac{R_3}{A_1^2 A_2^2}$$



$$R_{eq} = R_1 + R_2' = R_1 + \frac{R_2}{A_1^2} + \frac{R_3}{A_1^2 A_2^2}$$

# Addition of noise in cascaded amplifiers

The first stage of a two stage amplifier has output resistance of  $20\text{ k}\Omega$ , voltage gain of 10, input resistance of  $500\ \Omega$  and equivalent noise resistance  $2000\ \Omega$ . The second stage has output resistance of  $400\text{ k}\Omega$ , voltage gain of 20, input resistance of  $80\text{ k}\Omega$  and equivalent noise resistance of  $10\text{ k}\Omega$ . Compute the equivalent input noise resistance of the two stage amplifier. Also compute the equivalent input noise voltage given that the bandwidth of the amplifier is  $10\text{ kHz}$  and the ambient temperature is  $300\text{ K}$ .

$$R_3 = 400\text{k}\Omega$$

$$R_2 = \frac{20 \times 80}{20 + 80} \text{ k}\Omega + 10 \text{ k}\Omega = 26 \text{ k}\Omega$$

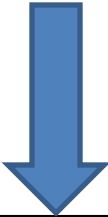
$$R_1 = 500\ \Omega + 2000\ \Omega = 2500\ \Omega.$$

$$\begin{aligned} R_{eq} &= R_1 + \frac{R_2}{A_1^2} + \frac{R_3}{A_1^2 A_2^2} \\ &= 2500 + \frac{26,000}{(10)^2} = \frac{400,000}{(10 \times 20)^2} \text{ ohms} = 2670\ \Omega \end{aligned}$$

$$\begin{aligned} V_{neq} &= \sqrt{4 k T B R_{eq}} = \sqrt{4 \times 1.38 \times 10^{-23} \times 300 \times 10^4 \times 2670} \text{ volt} \\ &= 0.677\ \mu\text{V}. \end{aligned}$$


# Signal to Noise Ratio (SNR)

- ❑ Purpose?
  - ❑ Comparing two system's performances
  - ❑ To know the relative signal strength at the same point



$$\frac{S}{N} = \frac{P_s}{P_n} = \frac{V_s^2/R}{V_n^2/R} = \left(\frac{V_s}{V_n}\right)^2$$

Noise Figure:



$$F = \frac{S/N \text{ at the input}}{S/N \text{ at the output}}$$

Greater than unity

>>> Noise Figure & Noise Temperature>>> Next Lecture>>>

# Q & A

